



UNIFIED COUNCIL

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UNIFIED CYBER OLYMPIAD - UC 329

Solutions for class : 9

Mental Ability

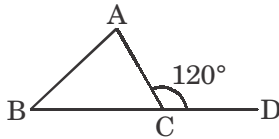
1. (A) Ratio of areas of adjacent faces of rectangular block = 900 cm²

$$lb.bh.hl = 900 \Rightarrow (lbh)^2 = 900$$

$$\therefore l.b.h = \sqrt{900} \Rightarrow lbh = 30$$

$$\therefore \text{volume} = 30 \text{ cm}^3.$$

2. (D) In $\triangle ABC$, $\angle ACD = 120^\circ$
Side BC produced to D.



$$\text{Let } \angle CAB = x^\circ$$

$$\angle ABC = \frac{2}{3} \angle CAB \text{ (given)}$$

$$\angle ABC = \frac{2}{3} x$$

$$\angle CAB + \angle ABC = \angle ACD$$

[\square an exterior angle of a triangle = sum of its two interior opposite angles]

$$x + \frac{2}{3} x = 120^\circ$$

$$\frac{3x + 2x}{3} = 120^\circ$$

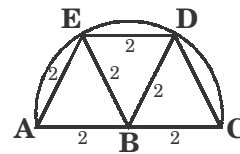
$$\frac{5x}{3} = 120^\circ \Rightarrow x = 120 \times \frac{3}{5} = 72^\circ$$

$$\text{Hence } \angle BAC = 72^\circ$$

3. (D) We know if $a + b + c = 0$ then $a^3 + b^3 + c^3 = 3abc$

$$\frac{a^2}{bc} + \frac{b^2}{ca} + \frac{c^2}{ab} = \frac{a^3 + b^3 + c^3}{abc} = \frac{3abc}{abc} = 3$$

4. (D) The 3 equilateral triangles which are inscribed in a semi-circle are $\triangle ABE$, $\triangle BDE$ and $\triangle BCD$



Here each side = 2 cm

$$\text{One triangle area} = \frac{\sqrt{3}}{4} a^2 = \frac{\sqrt{3}}{4} (2)^2$$

$$= \frac{\sqrt{3}}{4} \times 4 = \sqrt{3} \text{ cm}^2$$

$$\text{Total three triangles area} = 3 \times \sqrt{3}$$

$$= 3\sqrt{3} \text{ cm}^2$$

5. (C) $CD \parallel EF \parallel l_1$

$$\text{Now, } \angle x (180^\circ - 130^\circ) + (180^\circ - 132^\circ) = 50^\circ + 48^\circ + 98^\circ$$

$$\therefore \angle y (180^\circ - 130^\circ) + 30^\circ$$

$$= 50^\circ + 30^\circ + 80^\circ$$

6. (A) We know that,

$$\angle BOC = 90^\circ + \frac{1}{2} \angle A$$

$$\text{and } \angle BO'C = 90^\circ + \frac{1}{2} \angle A$$

$$\Rightarrow \angle BOC - \angle BO'C = \angle A$$

$$\therefore \angle BOC = \angle BO'C + \angle A$$

7. (D) Let $f(x) = px^3 + x^2 - 2x - q$
 When $f(x)$ is divisible by $(x - 1)$ then
 $f(1) = 0 \Rightarrow p(1)^3 + (1)^2 - 2(1) - q = 0$
 $\Rightarrow p + 1 - 2 - q = 0$
 $\Rightarrow p - q = 1 \dots\dots\dots (1)$

When $f(x)$ is divisible by $(x + 1)$ then
 $f(-1) = 0 \Rightarrow p(-1)^3 + (-1)^2 - 2(-1) - q = 0$
 $\Rightarrow -p + 1 + 2 - q = 0$
 $\Rightarrow p + q = 3 \dots\dots\dots (2)$

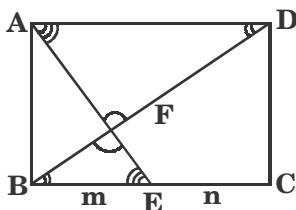
(1) + (2) $\Rightarrow p - q + p + q = 1 + 3$
 $\Rightarrow 2p = 4 \Rightarrow p = 2$ in (2)

(2) $\Rightarrow 2 + q = 3 \Rightarrow q = 3 - 2 = 1$

Hence $(p, q) = (2, 1)$

8. (D)

ΔFEB	ΔFAD
$\angle BFE =$	$\angle DFA$ (\because Vertically opposite angles)
$\angle FBE =$	$\angle FDA$ (\because Interior alternate angles)
$\angle BEF =$	$\angle DAF$ (\because Interior alternate angles)



$\therefore \Delta FEB : \Delta FAD$ (by AAA-similarity)

When two triangles are similar then the ratio of areas of two triangles is equal to the ratio of squares of any two corresponding sides.

Hence $\frac{\text{area}(\Delta FEB)}{\text{area}(\Delta FAD)} = \frac{BE^2}{DA^2} = \frac{FB^2}{FA^2} = \frac{FE^2}{FA^2}$

From the data given in question and by seeing figure, we can say

$BE = m$ and $DA = (m + n)$

$\therefore \frac{\text{area}(\Delta FEB)}{\text{area}(\Delta FAD)} = \frac{BE^2}{DA^2} = \frac{m^2}{(m + n)^2}$

9. (C) General form of the line parallel to Y-axis and K units away from it is $x = K$ Here given K = 5 units

\therefore Required equation $x = 5$

10. (D) Linear expression divided by $(1 + a + a^5)$ and $(1 + a^4 + a^5)$ individually only if the highest power of a is 10 (i.e. 5 + 5) and 9 (i.e. 5 + 4) both are positive. Clearly, in options (A) and (C), the highest power of a is a 8. So, these options are not correct. Now, we have option (D) in which both a^{10} and a^9 are positive.

11. (D) Let a, b, c be the sides of the triangle

Given perimeter = 42 cm

$\Rightarrow a + b + c = 42$ cm

$\Rightarrow 18 + 10 + c = 42$

(Given a = 18 cm and b = 10 cm)

$\Rightarrow c = 42 - 28 = 14$ cm

Now area = $\sqrt{s(s-a)(s-b)(s-c)}$

$\left[s = \frac{a+b+c}{2} = \frac{18+10+14}{2} = 21 \right]$

$= \sqrt{21(21-18)(21-10)(21-14)}$

$= \sqrt{21 \times 3 \times 11 \times 7}$

$= \sqrt{7 \times 3 \times 11 \times 7}$

$= 7 \times 3 \times \sqrt{11}$

$= 21\sqrt{11}$ cm²

12. (B) $\frac{x^2}{\sqrt{x^2 + y^2} + y}$

RF of $\sqrt{x^2 + y^2} + y$ is $\sqrt{x^2 + y^2} - y$

Multiply and divide by RF

$= \frac{x^2}{(\sqrt{x^2 + y^2} + y)} \times \frac{(\sqrt{x^2 + y^2} - y)}{(\sqrt{x^2 + y^2} - y)}$

$= \frac{x^2(\sqrt{x^2 + y^2} - y)}{(\sqrt{x^2 + y^2})^2 - (y)^2}$

$= \frac{x^2(\sqrt{x^2 + y^2} - y)}{x^2 + y^2 + y^2}$

$= \frac{x^2(\sqrt{x^2 + y^2} - y)}{x^2}$

$= \sqrt{x^2 + y^2} - y$

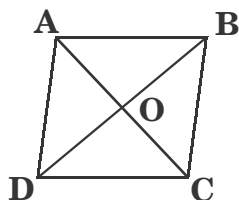
Reasoning

13. (B) On X-axis each small division = $\frac{1}{6}$ units
 On Y-axis each division = 1 unit
 \therefore point 'M' X-co ordinate = $18 \times -\frac{1}{6} = -3$
 point 'M' Y-co ordinate = $1.5 = \frac{3}{2}$

Hence point 'M' = $\left(-3, \frac{3}{2}\right)$

14. (A) $x^2 + 4y^2 + 4y - 4xy - 2x - 8$
 $(x^2 + 4y^2 - 4xy) - 2x + 4y - 8$
 $(x - 2y)^2 - 2(x - 2y) - 8$
 Let $x - 2y = k$
 $k^2 - 2k - 8$
 $k^2 - 4k + 2k - 8$
 $k(k - 4) + 2(k - 4)$
 $(k - 4)(k + 2)$
 $(x - 2y - 4)(x - 2y + 2)$

15. (A) Since, ABCD is a rhombus, so its all sides are equal.



Now, $BC = DC$

In $\triangle BDC$,

$$\angle BDC = \angle DBC = x^\circ$$

Also, $\angle BCD = 60^\circ$ [given]

$$\therefore x + x + 60^\circ = 180^\circ$$

$$\Rightarrow x = 60^\circ$$

$$\therefore \angle BDC = \angle DBC = \angle BCD = 60^\circ$$

So, $\triangle BDC$, is an equilateral triangle.

$$\therefore BD = BC = a$$

$$AB^2 = OA^2 + OB^2$$

[\square diagonals of rhombus intersect each other at 90°]

$$\Rightarrow OA^2 = AB^2 - OB^2$$

$$\Rightarrow OA^2 = a^2 - \left(\frac{a}{2}\right)^2 = a^2 - \frac{a^2}{4} = \frac{3a^2}{4}$$

$$\therefore OA = \frac{\sqrt{3}}{2} a$$

Now, $AC = \left(2 \times \frac{\sqrt{3}}{2} a\right) = \sqrt{3} a$

$$\therefore AC : BD = \sqrt{3} a : a = \sqrt{3} : 1$$

16. (B) First figure is vertically inverted to obtain the second figure. On following this pattern, we see that, option (B) will complete the second pair.

Hence, option (B) is correct.

17. (A) The stripes in small circles over large circles remain the same. The other elements in bigger circle i.e. star, dot and square are rotating in clockwise direction and the S written in small circle is rotating 90° in clockwise direction. On following this pattern, we see that option (A) will come next.

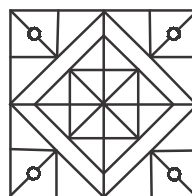
Hence, option (A) is correct.

18. (D) The figures (A), (B) and (C) have triangle upside down but option (D) does not follow this pattern.

So, option (D) is odd one out.

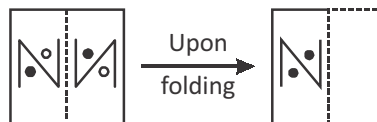
Hence, option (D) is correct.

19. (D) The grid can be completed as



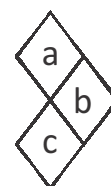
Hence, option (D) is correct.

20. (C) Upon folding, the transparent sheet will appear as



Hence, option (C) is correct.

21. (C) Consider the given figure as



Apply the logic, $\frac{a^2 + b^2}{10} = c$

From the first figure:

$$\frac{(11)^2 + (13)^2}{10} = \frac{121 + 169}{10} = \frac{290}{10} = 29.$$

From the second figure:

$$\frac{(17)^2 + (19)^2}{10} = \frac{289 + 361}{10} = \frac{650}{10} = 65.$$

In the same way, from the third figure:

$$\frac{(23)^2 + (29)^2}{10} = \frac{529 + 841}{10} = 137.$$

22. (B) When the given sheet (x) is folded, pairs of opposite faces are

(x, ●), (□, □) and (≡, †)

Clearly, the cubes shown in figures (ii) and (iv) consist of faces which are not formed when the sheet (x) is folded. So, these two cubes cannot be formed. Only the cubes given in figures (i) and (iii) can be formed.

Hence, option (B) is correct.

23. (C) In each row the figure in the first column is divided into two parts in the second column and into four parts in the third column.

Hence, option (C) is correct.

24. (B) Here, the first figure of the first pair is laterally inverted to obtain the second figure as shown

Following the above pattern, we see that option (A) will complete the second pair as

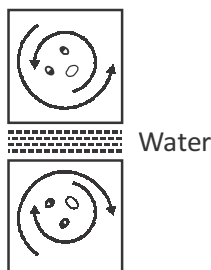
Hence, option (B) is correct.

25. (B) Figure (P) is same as figure (R). Similarly, figure (S) is same as figure (T) but figure (Q) is different.

So, figure (Q) is odd one out.

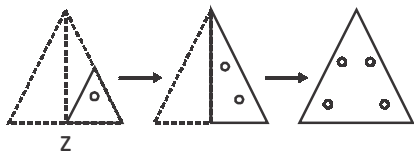
Hence, option (B) is correct.

26. (C) The water image can be obtained as



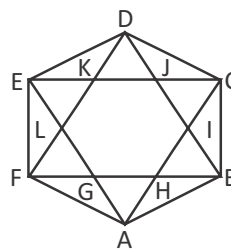
Hence, option (C) is correct.

27. (C) Upon unfolding the folded paper, represented by figure (Z), we get



Hence, option (C) is correct.

28. (C) On labelling the given figure, we get



Number of single triangles formed = $\Delta AGH, \Delta AHB, \Delta BHI, \Delta BIC, \Delta CIJ, \Delta CJD, \Delta DJK, \Delta DJE, \Delta EKL, \Delta ELF, \Delta FLG$ and $\Delta FGA = 12$

Number of triangles formed by 2 small triangles = $\Delta AGB, \Delta AIB, \Delta BHC, \Delta BJC, \Delta CID, \Delta CKD, \Delta DJE, \Delta DLE, \Delta EKF, \Delta EGF, \Delta FLA$ and $\Delta FHA = 12$

Number of triangles formed by 3 small triangles = $\Delta ABF, \Delta ABC, \Delta BCD, \Delta CDE, \Delta DEF$ and $\Delta AEF = 6$

Other bigger triangles = ΔACE and $\Delta BDF = 2$

\therefore Total number of triangles

$$= 12 + 12 + 6 + 2 = 32 \text{ triangles}$$

Hence, option (C) is correct.

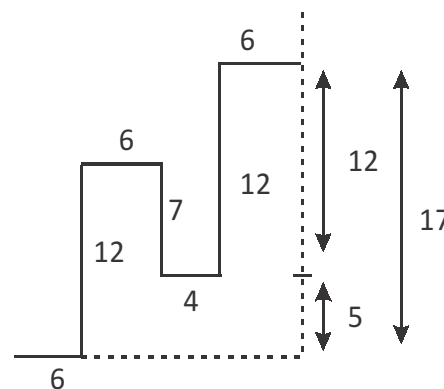
29. (D) $Q \times R = Q$ is the father of R.

$R \$ P = R$ is the brother of P.

$P \$ N = P$ is the brother of N.

Hence $Q \times R \$ P \$ N = P$ is the son of Q.

30. (A)



Computers

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|---------|---------|---------|
| 31. (C) | 32. (A) | 33. (C) |
| 34. (B) | 35. (D) | 36. (D) |
| 37. (B) | 38. (B) | 39. (B) |
| 40. (A) | 41. (C) | 42. (B) |
| 43. (B) | 44. (B) | 45. (D) |

English

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|---------|---------|---------|
| 46. (C) | 47. (D) | 48. (D) |
| 49. (B) | 50. (D) | |