

**01**

$\Delta ABC$ ,  $AB = BC = 29$  cm and  $AC = 42$  cm. What is the area of  $\Delta ABC$  ?

$$S = \frac{a + b + c}{2} = \frac{(29 + 29 + 42)}{2} \text{ cm} = 50 \text{ cm}$$

$$\begin{aligned} \Delta &= \sqrt{S(s - a)(s - b)(s - c)} = \sqrt{50 \times 21 \times 21 \times 8} \\ &= 21 \times \sqrt{50 \times 8} \\ &= 21 \times 20 = 420 \text{ cm}_2 \end{aligned}$$

**02**

The number  $N$  is a two digit numbers.

When ' $N$ ' is divided by 9 leaves a remainder 1.

When ' $N$ ' is divided by 10 leaves a remainder 3.

What is the remainder when ' $N$ ' is divided by 11 ?

73 satisfies the given two conditions

$$\begin{array}{r} 11)73(6 \\ \underline{66} \\ 7 \end{array}$$

Remainder '7' is 73 is divided by 11

**03**

What is the smallest whole number larger than are perimeter of any triangle with the sides of length 5 cm and side of 19 cm.

If 19 cm is considered as greatest side then third side must be 15 cm

[ $\therefore$  It is a whole number]

$$\therefore \text{Perimeter of the triangle} = 19 \text{ cm} + 5 \text{ cm} + 15 \text{ cm} \\ = 39 \text{ cm}$$

$$\therefore \text{The smallest whole number larger than the perimeter of the triangle} = 40 \text{ cm}$$

**04**

In triangle ABC, AD is drawn perpendicular to BC. If DC is greater than BD, show that AC is greater than AB.

Const:- Notice a point E on CD such that  $BD = DE$

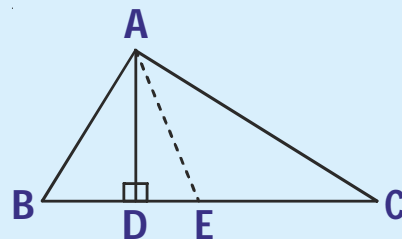
$\triangle ABD \cong \triangle AED$  [ $\therefore$  SAS congruency]

$$\Rightarrow \angle B = \angle AED \quad \dots\dots\dots (1)$$

$$\text{But } \angle AED = \angle C \quad \dots\dots\dots (2)$$

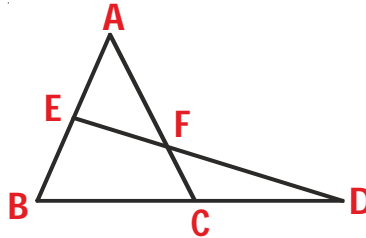
from (1) & (2)

$$\angle B > \angle C \Rightarrow AC > AB$$



**05**

In the following diagram,  $AB = AC$ . Prove that  $AF > AE$ .



Given in  $\triangle ABC$ ,  $AB = AC$

$$\Rightarrow \angle B = \angle ACB = x$$

In  $\triangle CDF$ ,  $\angle CFD < \angle ACB$

$$\Rightarrow \angle AFE < x \quad \dots\dots\dots (1)$$

[ $\because$  Exterior angle is greater than each interior opposite angle]

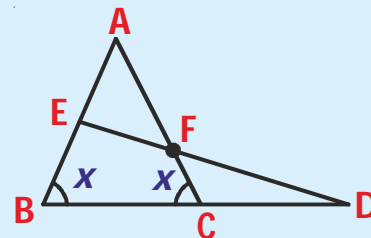
In  $\triangle BDE$ ,  $\angle AEF > \angle B$

$$\Rightarrow \angle AEF > x \quad \dots\dots\dots (2)$$

from (1) & (2)

In  $\triangle AEF$

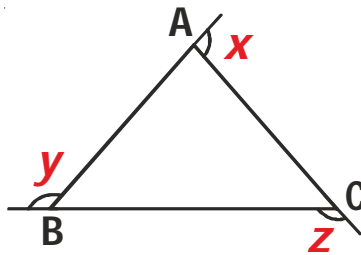
$$\angle AEF > \angle AFE \Rightarrow AF > AE$$



**06**

The following figure shows a triangle  $ABC$  with exterior angles as  $x$ ,  $y$  and  $z$ .

- (i) If  $AB > AC > BC$ ; arrange the angles  $x$ ,  $y$  and  $z$  in ascending order of their values.
- (ii) In the same figure, if  $y > x > z$ ; arrange sides  $AB$ ,  $BC$  and  $AC$  in descending order of their lengths.



- (i) Given  $\triangle ABC$ ,  $AB > AC > BC$   
 $\Rightarrow \angle ACB > \angle ABC > \angle BAC$   
 $\Rightarrow -\angle ACB < -\angle ABC < -\angle BAC$   
 $\Rightarrow 180^\circ - \angle ACB < 180^\circ - \angle ABC < 180^\circ - \angle BAC$   
 $\Rightarrow z < y < x$
- (ii)  $y > x > z \Rightarrow -y < -x < -z$   
 $\Rightarrow 180^\circ - y < 180^\circ - x < 180^\circ - z$   
 $\Rightarrow \angle ABC < \angle BAC < \angle ACB$   
 $\Rightarrow AC < BC < AB$   
 $\Rightarrow AB > BC > AC$