Foundation for Success

Unified International
Mathematics Olympiad

## UNIFIED INTERNATIONAL MATHEMATICS OLYMPIAD (UPDATED)



KEY

| 1 | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C | C | A | A | D | D | B | C | B | A |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| B | B | C | A | C | C | D | C | A | D |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| C | A | C | B | A | B | A | A | A | C |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| A | A | B | C | C | D | D | C | A | B |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| A | C | B | D | A | A | B | C | D | A |

## EXPLANATIONS

## MATHEMATICS

1. (C)


Option (C) has 6 lines of symmetry.
02. (C) $225 \mathrm{~g}+175 \mathrm{~g}+200 \mathrm{~g}+200 \mathrm{~g}+175 \mathrm{~g}+175 \mathrm{~g}$ $=1.15 \mathrm{~kg}$
So, no. of jars Rishi have $=6$ jars.
03. (A) No. of boxes $=5$

No. of marbles in each box $=19$
No. of boxes given to his friends $=2$
No. of marbles with Alekhya $=19 \times 3=57$
04. (A) Each division $=200 \mathrm{ml}$
water in the beaker $=1 l 200 \mathrm{ml}$
If 125 ml is poured out from the beaker
$=1200 \mathrm{ml}-125 \mathrm{ml}$
$=1075 \mathrm{ml}=1 \mathrm{l} 75 \mathrm{ml}$
05. (D) There are no parallel lines in a triangle.

06. (D) Equivalent fraction of $\frac{2}{5}=\frac{2 \times 2}{5 \times 2}=\frac{4}{10}$
07. (B) No. of red pens $=22$

No. of blue pens $=22 \times 3=66$
Total $=66+22=88$ pens.
08. (C) $3: 52$
09. (B) No. of books bought by Rahul $=8$

Amount paid to shopkeeper
= ₹ 50 + ₹ 50 = ₹ 100
Changed he received = ₹ 28
= ₹ 100 - ₹ 28 = ₹ 72
Cost of each book $=₹ 72 \div 8=₹ 9$
10. (A) $740 \mathrm{~cm}+17 \mathrm{~cm}$
$=757 \mathrm{~cm}=7 \mathrm{~m} 57 \mathrm{~cm}$
11. (B) ₹ $3820-₹ 1132=₹ 2688$ (Razak)
$₹ 10473$ - ₹ 3820 - ₹ 2688 = ₹ 3965
12. (B) $\frac{48}{60}=\frac{8}{10}=\frac{4}{5}$
13. (C) By 'guess and check' method

$$
\begin{array}{r}
555 \\
\times \quad 3 \\
\hline 1665 \\
\hline
\end{array}
$$

14. (A) $1-\frac{1}{10}-\frac{3}{5}=1-\frac{1}{10}-\frac{6}{10}=\frac{3}{10}$
15. (C) $2899+411=3310$ $3310 \approx 3300$
16. (C) Among $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}$ and $\frac{1}{5}, \frac{1}{5}$ is the smallest value and $\frac{1}{4}$ is the second smallest value. Therefore, the sum of these two fractions will have the smallest value.
17. (D) Multiples of 9: (9) $18,27,36$, 45) 54, 63, $72, \ldots$
18. (C) Sum: $7456+647=8103$
$8103+9=900$ R 3
Quotient: 900; Remainder: 3

(Note: It is important to add a 'zero' indicated at the arrows, when you cannot divide)
19. (A) Multiples of $6: 6,12,18,24,30,36$, $42,48,54,60,66,72,78, \ldots$

Multiples of 9: 9, 18, 27, 36, 45, (54), 63, 72, ...
$72=70$
The number is 72
20. (D) $128 \times 14=1792$
21. (C) CD and GH
22. (A) $1 l 345 \mathrm{ml}+8 l 875 \mathrm{ml}=9 l 1320 \mathrm{ml}$ $=10 l 321 \mathrm{ml}$

She used $10 l 321 \mathrm{ml}$ of water in all
23. (C) $4 \mathrm{~km} \mathrm{56m-3km} 187 \mathrm{~m}$
$=3 \mathrm{~km} 1056 \mathrm{~m}-3 \mathrm{~km} 187 \mathrm{~m}$
$=0 \mathrm{~km} 869 \mathrm{~m}$
Piyush travelled 869 m further from her house to the shopping mall than Tarun
24. (B) 3 months $\rightarrow 67 l$

1 month $\rightarrow 67 l \div 3$
$=22 \frac{1}{3} l$
12 months $\rightarrow 22 \frac{1}{3} l \times 12$
$=\frac{67}{3} l \times 12=268 l$
25. (A) 416

$$
\begin{array}{r}
1360 \\
+\quad 143 \\
\hline 503 \\
\hline
\end{array} \begin{array}{r}
4{ }^{49} Q^{9} 3 \\
-\quad 87 \\
\hline 416 \\
\hline
\end{array}
$$

Joy had 416 balloons at first
26. (B) $C+4 \mathrm{~kg}=\mathrm{B}$

This means $B$ is heavier than C by 4 kg .


2 units $\longrightarrow 8-4$
Mass of $\xrightarrow{=4 \mathrm{~kg}} 4 \div 2$

$$
=2 \mathrm{~kg}
$$

(You may also use guess and check to find the mass of C .)
27. (A) You have to observe and guess how the corner numbers have been arrived at.

| $1+2=3$ | $3 \times 3=9$ |
| :--- | :--- |
| $2+4=6$ | $6 \times 6=36$ |
| $3+5=8$ | $8 \times 8=64$ |
| $4+5=9$ | $9 \times 9=81$ |

The value of $X$ is 81
28. (A) Multiples of $2: 2,4,6, \ldots, 10,12,14, \ldots$, $20,22,24, \ldots, 30,32, \ldots$

Multiples of $3: 3,6,9,12,15,18,21,24$, 27, 30, ...

Multiples of 5: 5, 10, 15, 20, 25, 30, ...
The first common multiple of 2,3 and 5 is 30. Therefore, the least number of paper clips that can be shared equally among 2 , 3 and 5 girls without any remainder is 30

$$
46^{7} Q^{1} 18
$$

29. (A)

| -14663 |
| ---: |
| 32155 |

30. (C)

$3 \times 1=3$
$3 \times 2=6$
$3 \times 5=15$
$3+6+15=24$

$4 \times 1=4$
$4 \times 2=8$
$4 \times 6=24$
$4+8+24=36$
31. (A) $144=1 \times 144 \quad 1+144=145$
$2 \times 722+72=74$
$3 \times 483+48=51$
$4 \times 364+36=40$
$6 \times 246+24=30$

$9 \times 169+16=25$
$12 \times 12$
$12+12=24$
Summit's is 18 years old.
32. (A)

33. (B)

$30 \div 3=10 \mathrm{~cm}$
$30+30+10+30+10=110 \mathrm{~cm}$
34. (C) ₹ 98.26 - ₹ 32.60
= ₹ 97.126 - ₹ 32.60 = ₹ 65.66
₹ $65.66-₹ 27.88$ = ₹ $64.166-₹ 27.88$
= ₹ 37.78
₹ 98.26 - ₹ 32.60 = ₹ 27.88 + ₹ 37.78
35. (C) Perimeter of given figure is 16 cm


REASONING
36. (D) Each letter stands for an ascending numerical value, starting with one and ending with seven. Zero goes before One.

Zero One Two Three Four Five Six Seven Eight
37. (D) Opportunity and chance are similar words. Remaining option have opposite words.
38. (C) Bottom shape becomes large shape and rotate $90^{\circ}$. The top two shapes interchange their position. Middle image in the final figure rotate $180^{\circ}$.
39. (A) There are 12 cubes in the letter 0 .
40. (B)

41. (A)

42. (C)

43. (B)


All blue dots change to horizontal line, all white dots are unaffected
44. (D)

45. (A)


CRITICAL THINKING
46. (A)

47. (B)

48. (C)

|  | Singing | Dancing | Playing <br> Guitar |
| :---: | :---: | :---: | :---: |
| Rakesh | $\nearrow$ |  |  |
| Pandu |  |  |  |
| Saranya |  |  | $\nearrow$ |
| Jim |  |  | $ل$ |
| Sravan |  | $\nearrow$ |  |

49. (D) I feel thankful to him.
50. (A) At the end of the first ramp the ball will be moving vertically, and so will fall back down, eventually coming to rest at the lowest point (P).
